

Incompressible fluid

$$A_1 v_1 = A_2 v_2$$

$$A_1 \frac{dh}{dt} = -A_2 \sqrt{2gh}$$

$$\frac{dh}{dt} = -\frac{A_2}{A_1} \sqrt{2g} \sqrt{h}$$

$$k = \frac{A_2}{A_1} \sqrt{2g}$$

$$\frac{dh}{dt} = -k \sqrt{h}$$

$$\int \frac{1}{\sqrt{h}} dh = -\int k dt$$

$$2\sqrt{h} = -kt + C$$

$$\sqrt{h} = \frac{-kt}{2} + C$$

$$h(t) = \left(\frac{-kt}{2} + C \right)^2$$

$$h(0) = h_0 = C^2, \quad C = \sqrt{h_0}$$

$$h(t) = \left(\frac{-kt}{2} + \sqrt{h_0} \right)^2$$

$$mgh = \frac{1}{2} m v_1^2 + \frac{1}{2} m v_2^2$$

v_1 = velocity of water at the top

v_2 = velocity of water coming out of hole

$$v_2 \gg v_1$$

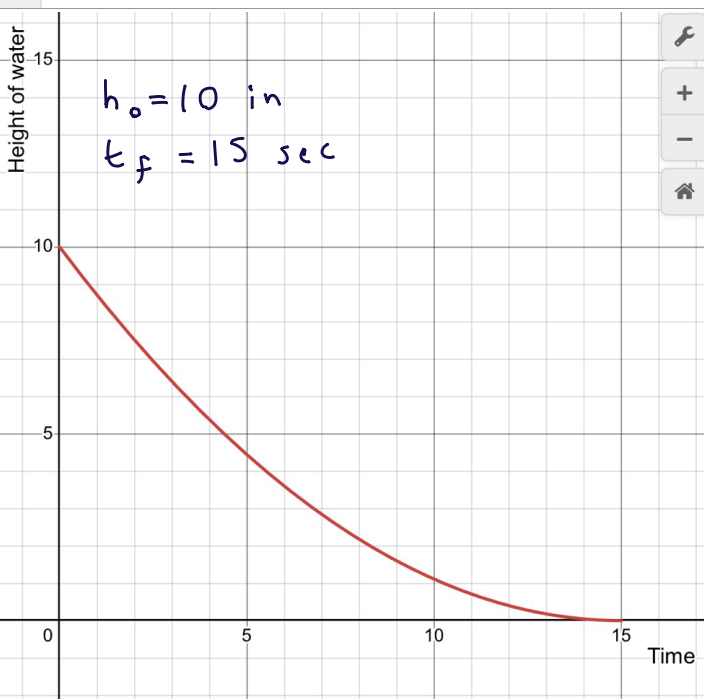
$$mgh \approx \frac{1}{2} m v_2^2$$

$$gh = \frac{1}{2} v_2^2$$

$$v_2 = \sqrt{2gh}$$

RATE OF CHANGE OF VOLUME $\propto \sqrt{h}$

$$h = \left(\frac{-\sqrt{10}t}{15} + \sqrt{10} \right)^2 \{0 < t < 15\}$$



k can be determined experimentally by measuring time to empty the tank, t_f

$$h(t_f) = 0 = \left(\frac{-kt_f}{2} + \sqrt{h_0} \right)^2$$

$$\frac{-kt_f}{2} + \sqrt{h_0} = 0$$

$$k = \frac{2\sqrt{h_0}}{t_f}$$

$$h(t) = \left(\frac{-\sqrt{h_0}t}{t_f} + \sqrt{h_0} \right)^2$$